Experimental Evaluation of a Novel Sensor-Based Sorting Approach Featuring Predictive Real-Time Multiobject Tracking

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Abstract—Sensor-based sorting is a machine vision application that has found industrial application in various fields. An accept-or-reject task is executed by separating a material stream into two fractions. Current systems use line-scanning sensors, which is convenient as the material is perceived during transportation. However, line-scanning sensors yield a single observation of each object and no information about their movement. Due to a delay between localization and separation, assumptions regarding the location and point in time for separation need to be made based on the prior localization. Hence, it is necessary to ensure that all objects are transported at uniform velocities. This is often a complex and costly solution. In this paper, we propose a new method for reliably separating particles at non-uniform velocities. The problem is transferred from a mechanical to an algorithmic level. Our novel advanced image processing approach includes equipping the sorter with an area-scan camera in combination with a real-time multiobject tracking system, which enables predictions of the location of individual objects for separation. For the experimental validation of our approach, we present a modular sorting system, which allows comparing sorting results using a line-scan and area-scan camera. Results show that our approach performs reliable separation and hence increases sorting efficiency.

Index Terms—Automated visual inspection, machine vision, real-time multiobject tracking, sensor-based sorting.

I. INTRODUCTION

SENSOR-BASED SORTING is a machine vision application that is of high relevance in various industrial fields. Commonly, the task can be understood as performing an accept-or-reject decision with the goal to detect and remove defect, faulty, low-quality or foreign items from a stream of material in a production line [1]. Corresponding systems are typically used for quality inspection. The particular motivation depends on the field of application. For instance, in the field of mineral processing, the efficient extraction and recovery of raw materials is crucial due to limited existing reserves. Examples include the sorting of porphyry copper [2], quartz, magnesite and gold ores [3], [4]. In food processing, products, e.g., dried vegetables, fruits [5] and nuts [6], often need to be cleaned from foreign, potentially dangerous objects as well as low-quality and damaged entities. Furthermore, sensor-based sorting solutions are a key technology in recycling and are often implemented as part of waste processing with the goal to separate materials for reuse [7]. For instance, recent works propose usage for automated sorting of plastic flakes [8] and electronic waste [9]. In an industrial application, systems typically run twenty-four hours a day, seven days a week, consequently handling massive amounts of the goods to be sorted. Hence, any improvements in sorting efficiency already have enormous economic and ecologic impact due to the large quantities involved.

A. Functional Principle

A schematic illustration of sensor-based sorting systems is provided in Fig. 1. Obviously, the design and implementation involves several disciplines and has hence attracted research from various perspectives. From an abstract point of view, the material is fed into the system onto a transportation mechanism, for instance a conveyor belt or chute. Although best practice strategies have been acquired, for instance as presented in [10] regarding chutes, design choices typically depend on the product to be sorted. Along the way, the material is perceived by one or multiple sensors, possibly in combination with an appropriate illumination device as for optical sensors [11]. State-of-the-art systems use line-scanning sensors for this purpose. Perception can take place either after the material has been discharged from the transport mechanism, as illustrated in Figs. 1(a) to 1(c), or while it is still on it,
In theory, an arbitrary number of classes can be distinguished after classification is performed on the basis of certain features, e.g., color and regions containing individual objects are extracted. Classification and actuator control. With respect to real-time requirements, firm deadlines apply for the deflection of objects since the actuators need to be triggered exactly when the objects pass the separation stage. Hence, a fixed delay between perception and separation is assumed for all particles. However, in the case of objects that are to be removed from the stream, a prediction needs to be performed when and where they will reach the separation stage. The choice of an appropriate sensor depends on the sorting task and the material’s classification criteria at hand. Typically, the image data needs to be preprocessed in a first step. Following that, the image is segmented and regions containing individual objects are extracted. Classification is performed on the basis of certain features, e.g., color or geometry related, and a sorting decision is derived. The decision is carried out by means of a separation mechanism. In theory, an arbitrary number of classes can be distinguished at the detection stage and separation into several fractions is possible. However, in industrial applications, the task is preferably realized as a binary sorting task, i.e., product and residues, since multi-way sorting requires complex mechanical handling.

For the successful application of sensor-based sorting, the feed material is typically preconditioned in terms of using defined particle size distributions, which can be obtained via screening, for instance. Especially for small, cohesive materials, physical separation is typically performed using an array of compressed air nozzles [21], [22]. The minimum particle size that can be handled by a system is limited by the pneumatic resolution, proximity between objects and characteristics of the material transport. The system needs to be capable of deflecting single particles without causing any disturbances such as turbulence of other particles. For larger products, electro-mechanical fingers or robot arms are also used. However, in this paper, we focus on pneumatic separation.

There are two main types of errors that can occur during the sorting process, potentially leading to a sorting error. The first type are errors in material recognition. In case of such an error, the data analysis reaches a wrong conclusion regarding the classification of a particle, which, for instance, can lead to the sorting decision of rejection although the particle was to be accepted. The second type are errors in material separation. Here, a correct sorting decision is derived, yet the particle is not physically removed from the product, for instance due to poor control of the actuator. This is the type of error we focus on in this paper, the recognition error is not considered.

### B. Problem Formulation and Contribution

Besides the actual conveyance, the transportation phase aims at creating a monolayer of the material, i.e., avoid that particles lie on top of each other, decreasing proximity between individual objects, i.e., avoid the formation of clusters, and achieving ideal flow control. Creating a monolayer ensures that no occlusions occur. Avoiding proximity is important for the deflection of individual objects, since the pneumatic resolution, both spatial and temporal, is limited and co-deflections of objects, i.e., the unwanted deflection of objects nearby an object that is to be deflected, are to be avoided. Ideal flow control means that all objects shall be accelerated to the same velocity, whereas velocity perpendicular to transport direction should be eliminated. This is crucial since there exists a temporal gap between the perception and the separation of the material, which is caused by the delay introduced by the required data processing, see Fig. 2. Localization is performed during perception and hence prior to separation. Due to usage of a line-scanning sensor, only a single image is available for each object. Therefore, no information regarding the motion of an object can be derived. Yet, in order to safely deflect objects that are to be removed from the stream, a prediction needs to be performed when and where they will reach the separation stage. Hence, a fixed delay between perception and separation is assumed for all particles. However, in the case of objects for which this assumption does not apply, an error may occur during separation, see Fig. 3(a).

One approach to minimizing this error is to place the scan line as close as possible to the separation line. Although

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**Fig. 1.** Schematic illustration of common types of sensor-based sorting systems. The green objects represent particles to be accepted and the red ones those to be removed from the stream. The yellow ray denotes the field of view of the sensor and the blue ray the compressed air released to deflect an object. In Figs. 1(a) to 1(c), detection of particles happens during the flight phase. In contrast, in Fig. 1(d), detection happens on the transportation device.
response times of sensors and processing systems are decreasing due to new developments, the distance cannot be arbitrarily minimized. Due to the firm real-time requirements, even in times of high system load caused by high material throughput, data processing needs to be completed before the material passes the separation stage. Even a few milliseconds of delay can cause the estimated position to differ from the actual position if there is no ideal flow control.

For certain materials, achieving optimal flow control is rather hard. A common strategy to increase the reliability of deflecting unwanted objects is to enlarge the deflection window, i.e., activate more nozzles longer than supposedly needed. However, this implies two major disadvantages. Firstly, the risk of falsely co-deflecting objects increases. Secondly, the amount of compressed air required to deflect the object increases. The latter is particularly noteworthy considering the high energy demand and hence costs associated with the usage of compressed air [23]. In [24], it is estimated that about 70% of the operational costs of sensor-based sorting systems is caused by compressed air and air extraction. A mechanical solution to the problem is the application of very long conveyor belts in order to gain more time during transportation for the material to come to rest. However, this solution is quite costly in terms of purchase costs, maintenance and required space. Chutes are a much cheaper way of realizing transportation. In turn, achieving optimal flow control is comparatively hard. The texture and size of the contact surface of an individual object strongly impacts its motion along the chute.

In this paper, we demonstrate how deviations in transport velocity can be handled by our advanced image processing approach instead of mechanical components. We present a sorting system equipped with an area-scan camera, a predictive real-time multiobject tracking system and provide experimental results for the sorting efficiency in comparison with a conventional line-scan camera setup as contrasted in Fig. 3. Our system enables accurate, individual estimates per object where it is moving and even allows deriving information about how it is moving. Recent advances in CMOS camera technology support the suitability of our system for industrial application on a large scale. To our best knowledge, this is the first time a corresponding system was implemented and results of real sorting experiments are presented.

C. Related Work

The problem of tracking multiple objects has attracted intensive research over several decades, especially in the field of computer vision [25]. There exists a huge diversity of applications from different specialist areas in which input data for the tracking system is generated by an imaging sensor. Corresponding systems can be used to count entities in the field of view whereas entities appear and disappear over time, for instance fish in underwater videos [26], vehicles for traffic flow surveillance [27] or people in video security applications [28]. Dependent on the system implementation, predictions of future events can be derived, for instance collisions at traffic intersections [29]. In the context of quality control in an industrial setting, a system is proposed in [30] in which sputters are tracked during a laser-welding process. The system works at a comparatively high frame rate and has the purpose to detect only sputter events that are strong enough to be critical to the welding process. In the context of sensor-based sorting, utilizing multiobject tracking was first proposed in [31]. Using a simulation-driven approach [32], it was shown that predictive tracking can decrease the error in physical separation [33], [34].

Besides the mere detection and prediction of future events, tracking objects can also serve the purpose to perform quality assessment directly based on the motion behaviour. Many works exist in the field of computer-assisted sperm analysis, both regarding animal [35] and human sperm quality [36]. The data from the tracking is here used to measure the motility of individual spermatozoa, which is an important characteristic for the quality assessment [37]. In ecoinformatics, motion features exist in the field of computer-assisted sperm analysis, both regarding animal [35] and human sperm quality [36]. The data from the tracking is here used to measure the motility of individual spermatozoa, which is an important characteristic for the quality assessment [37]. In ecoinformatics, motion features can be used to classify certain species, for instance birds [38]. In [39], [40], tracking has also been proposed to utilize motion-based features for the characterization of materials in sensor-based sorting. This approach can enable the discrimination of optically identical products, although an optical sensor is used.

Many works exist discussing problems in characterization of materials in sensor-based sorting. However, evaluation
of sorting systems from an holistic point of view appear to be rather rare. In [41], the authors propose a definition of separation efficiency and utilize it to quantify sorting performance as a function of the proximity of objects in the material feed. They further investigate different feed characteristics by means of a Monte Carlo simulation and quantify results based on their prior introduced definition of sorting efficiency in [42]. Following the concept of receiver-operating characteristic (ROC) curves, the idea of a sorting optimization curve (SOC) is presented in [43]. SOCs are intended to support the choice of an operating point based on yield and quality factors and predict the sorting quality. In [3], the authors adapt the conventional approach of confusion matrices, which are typically used to evaluate a classifier, to sensor-based sorting. This enables the usage of well-known figures of merit such as accuracy, specificity and sensitivity.

II. METHODS AND MATERIALS

In this section, we provide a description of the methodological approach and the experimental platform that was designed for this study. In Sec. II-A, we outline the tracking system developed for sensor-based sorting. Following that, Sec. II-B introduces the sorting system designed for the evaluation.

A. Predictive Real-Time Multiobject Tracking

In contrast to conventional systems, which use line-scanning sensors, our system is based on the application of an area-scan sensor. The difference regarding the format of the obtained image data is illustrated in Fig. 4. When using line-scanning sensors, several lines recorded at consecutive time points are merged in order to obtain a 2D image [44]. Hence, over time, an image of infinite length is formed. In turn, using an area-scan sensor yields a stack of 2D images. The crucial difference is that using the area-scan sensor, individual objects can be detected at several time points, while line-scan sensor systems only obtain a single observation. In order to be able to track multiple objects simultaneously, the correspondences of objects in consecutive frames need to be determined. More precisely, for application in sensor-based sorting, several thousand objects need to be tracked concurrently. Hence, a multiobject tracking algorithm is used.

Individual objects in the feed are detected using image processing. More precisely, color-based segmentation in HSI color space is performed in order to convert a recorded color image in a segmentation image that partitions the image in multiple segments. Pixels belonging to the background are encoded with 0, while any other value represents a certain color class. In the course of this study, we define intervals for all three color components, i.e., hue, saturation and intensity, to perform the segmentation. As depicted in Fig. 5(a), segmentation into back- and foreground can be preformed by defining a threshold for the saturation. A threshold for the hue enables distinguishing between different classes of objects, see Fig. 5(b). Including the intensity further improves the result.

Since there are typically several objects in an image, individual objects are identified using connected component analysis with an 8-connected neighbourhood. Using this representation, we calculate the centroid. For an object covering \( n \) pixels with 2D coordinates \( p_i, i = 1, \ldots, n \), the centroid is calculated by \( \frac{1}{n} \sum_{i=1}^{n} p_i \). The resulting point object serves as the input for the tracking algorithm. Hence, we perform point tracking, which is a common approach for tracking small objects in images [25].

In accordance to the categorization proposed in [45], our system implements a detection-based tracking approach with deterministic output. Moreover, results of the tracking are required in real-time. Therefore, online tracking is performed, i.e., images are handled sequentially. We further refer to the system as predictive tracking since it enables predicting the point in time and position for the deflection of a particle. A schematic overview of the system is provided in Fig. 6.

For each object, a standard Kalman filter is used as an estimator, using the 2D position \((x, y)\) and the velocities in both directions, i.e., \((v_x, v_y)\), as state variables. When the assignments between measurements and tracks are known, knowledge about the positions of the objects is refined by performing a Kalman filter update step for each individual object. For the prediction step, we apply a linear motion model, more precisely a constant velocity model [46]. The underlying assumption of this model is that changes to the velocity are relatively small. For simplicity, the acceleration
Fig. 6. Detailed view on the data processing block from Fig. 2. The system sequentially receives color images, which are first segmented based on color. Connected component analysis is then performed in order to identify individual objects in the image. The centroids of these objects serve as the input for the multiobject tracking system. The tracking system performs predictions for the currently existing tracks and identifies the correspondences between the predictions and centroids of the current frame. It handles newly appeared and disappeared objects and provides the prediction for the separation.

affecting the velocity is modeled as white noise, i.e., we assume the actual accelerations are temporarily independent and distributed according to the same probability distribution in every time step. It is important to note that the parameters of a motion model are estimated for each tracked object individually in each time step according to the movement observed so far. The complexity of the prediction step is $O(n)$ with $n$ denoting the number of current tracks.

The point correspondences, i.e., the associations between predictions and measurements of the current frame, are identified by solving the linear assignment problem

$$
\min \sum_{i=1}^{N} \sum_{j=1}^{M} a_{i,j} x_{i,j} \\
\text{s.t.} \quad \sum_{j=1}^{M} x_{i,j} = 1, \ i = 1, \ldots, N \\
\sum_{i=1}^{N} x_{i,j} = 1, \ j = 1, \ldots, M,
$$

where $N$ and $M$ represent the number of predictions and measurements, respectively. The cost function $a$ is implemented as the Mahalanobis distance. The constraints guarantee a one-to-one assignment. This problem needs to be solved for each frame and causes the main computational burden within the tracking algorithm. Due to its suitability for parallelization, we use the Auction Algorithm [47] for this purpose. An example image sequence highlighting results of the detection and tracking stages is provided in Fig. 7.

In each time step, we estimate the remaining time until an object will reach the separation stage. Whenever this estimated time gap reaches a certain threshold, the estimated point in time as well as position when the object reaches the separation stage is calculated and transmitted to the separation device. This threshold needs to be solved for each frame and causes the main computational burden within the tracking algorithm. Due to its suitability for parallelization, we use the Auction Algorithm [47] for this purpose. An example image sequence highlighting results of the detection and tracking stages is provided in Fig. 7.

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algorithm is capable of solving the association problem for about 1000 objects at around 200 Hz on a modern GPU. The algorithm is further robust against missed and faulty detections, which may be caused by occlusions, collisions are poor objects detection. This is achieved by implementing a scoring system for the creation of new tracks as well as the deletion of existing tracks. Each newly created track is assigned an initial score, which is increased whenever a measurement is assigned to the track until a defined maximum score is reached. In turn, if no measurement of a frame is assigned to the track, the score is decreased. In case the score drops below zero, the track is deleted. New tracks are created for measurements that have not been assigned to a track.

B. Experimental Optical Sorting Platform

For the validation of our approach, alterations on the hardware of the sorting system are required. More precisely, the system needs to be equipable both with a line-scan and an area-scan camera as well as the corresponding illumination devices. Therefore, for our experiments, we developed a system that enables rapid prototyping in this respect. A photo of the resulting construction is provided in Fig. 8.

a) General design: The basis of the sorting system is the back panel. It is realized as a mechanical breadboard and contains equidistant perforations that are intended for mounting different components. The distance between two perforations is 25 mm, both horizontally and vertically. The size of the board used in this study is 142 cm × 102 cm. Adapters are designed to build an interface between the back panel and commercially available components.

An electromagnetic feeder, annotated by 1 in Fig. 8, is used to feed material into the system. It runs at a constant frequency of 50 Hz. The amplitude is configurable via a controller containing a potentiometer and is monitored using a vibration sensor. The latter ensures a constant feeding rate, for instance independent of the temperature of the electromagnetic feeder. The chute considered in this study has a total length of 31 cm and width of 15 cm, see annotation 2 in Fig. 8. It is made of cold-rolled steel and hence has a plain and even surface. The illumination for use with a line-scan camera (see 3a in Fig. 8) consists of two line-shaped LED bars which are indicated by 3b in Fig. 8. It is mounted at a position such that the material is observed after falling off the chute. For usage with the area-scan camera, an LED ring light with an inner diameter of 21 cm is used. The observation area and consequently the position of the ring light is located at the end of the chute, see Fig. 7. In both cases, the bright field illumination is mounted above the material stream such that the reflected light is captured by the camera. Separation of the material is performed by fast switching compressed air valves. The system contains an array of 16 valves covering a distance of 16 cm which can be activated individually, see 4 in Fig. 8. Hence, the spatial pneumatic resolution is 10 mm. The pressure can be controlled using a pressure regulator. The individual valves are accessed via a Controller Area Network (CAN). The speed of communication over the data channel, i.e., the baud rate, is 1000 bd.

b) Image acquisition: For the comparison of sorting efficiency, experiments are carried out with a line-scan and an area-scan camera. In both cases, the reflected light from the particles is captured by the camera sensor. This can be used to measure color features. The line-scan model used is e2v AViiVA SC2, which offers 1365 px at a maximum line rate of 14.8 kHz. The area-scan model used is Allied Vision Bonito CL-400 color camera, which offers a maximum resolution of 2320 × 1726 px at 192 Hz. For both cameras, we use the Zeiss Classic lense Planar T 1.4/50 ZF.2. Both cameras are connected to a computer using the Camera Link interface. Therefore, the computer is also equipped with a programmable frame grabber from the microEnable 4 series from Silicon Software. Several image pre-processing steps are performed directly on the grabber, such as shading, demosaicing (for the area-scan camera) and generation of the segmentation image.

c) Processing computer system: The computer system is equipped with an Intel i7-5960X CPU and 16 GB RAM. Furthermore, it contains a NVIDIA GeForce GT 740 GPU on which the association step for multioject tracking is performed. The operating system is Microsoft Windows 7 64-bit.

III. TEST METHODOLOGY

In order to allow a fair comparison between the conventional and our proposed approach, we ensure that all operational sorting parameters are fixed except for the changes to components
owed to the approaches themselves, e.g., illumination, sensor and data processing. This implies that we are not interested in presenting an optimal sorting solution for a specific product, but rather in demonstrating that the proposed approach can increase sorting performance in a relative fashion. In the following subsections, the relevant sorting parameters considered in the study are described.

A. Characteristics of the Material Stream

We perform sorting experiments for two artificially labeled products: wooden plates and dry lentils, see Fig. 9. The products were deliberately chosen due to major differences in geometry and movement behavior on the chute. More precisely, the wooden plates represent a very homogeneous and the lentils a highly heterogeneous product in terms of the shape of individual particles. A thorough description of the wooden plates can be found in [32]. Their volume is $2 \text{mm} \times 5 \text{mm} \times 6 \text{mm}$. The plates are artificially separated into two fractions by coloring, whereas some plates are kept wooden and some are colored blue. Being a natural product, the volume of the lentils is diverse. However, most lentils have a diameter of approximately $4 \text{mm}$. In order to derive a sorting decision, we include yellow and red lentils in the material stream. Hence, for both products, a significant difference in color exists to discriminate the product into two fractions. For our experiments, this allows us to neglect recognition errors because they do not occur and solely measure the error in physical separation.

An experiment carried out consists of sorting $200 \text{g}$ of the product in a batch-wise manner. The mass flow of the material in our scenario depends on the amplitude of the feeder. We investigate a single configuration of the feeder that results in a similar mass flow for both products. The mass flow was determined experimentally by feeding material through the system onto a digital weighing scale, which is connected to a computer in order to record the measured values over time at a temporal resolution of approximately $18 \text{Hz}$. After starting the feeding process, the mass flow increases over time until reaching approximately $5 \text{g/s}$. Most of the time of the sorting process, the feeding rate remains in this state. When only little material is left in the feeder, the mass flow decreases until no material is left. With respect to the amount of material to be deflected, we consider a ratio of $5\%$. The impact of the mass flow and ratio to be deflected on sorting performance has already occasionally been investigated in the literature, e.g., in [41], [42].

B. Sensor and Software Parameters

We configure the line-scan camera to run at approximately $7682 \text{Hz}$ using a width of $446$ pixels. Due to the high required data transfer rate and the resulting computational burden, we restrict the area-scan camera to approximately $93 \text{fps}$. Consequently, the entire data processing, i.e., demosaicing the Bayer pattern, color segmentation, connected component analysis, descriptor extraction, tracking, classification and transfer of deflection patterns, is granted a processing time of approximately $10 \text{ms}$ on average. Furthermore, the image is cropped to a width of $2208$ pixels. For the area-scan camera, we report a spatial resolution of approximately $69.58 \mu \text{m}$ and for the line-scan camera of $359.65 \mu \text{m}$. It is important to note that the difference is negligible as for both cases the spatial resolution is many times higher than the pneumatic spatial resolution.

The deflection pattern describes which nozzles are to be triggered during which time interval. There exist different approaches how the pattern can be calculated [49]. As also done in [42], we use the common approach of using the bounding box of an object to be deflected to calculate the deflection pattern. However, we consider two configurations. The first configuration corresponds to the bounding box of the object as detected in the image and is referred to as small pattern in the remainder. The second configuration uses enlarged deflection patterns and is referred to as large pattern in the remainder. Here, the window is enlarged both in transport direction and perpendicular to it. In perpendicular direction, we enlarge the window on both sides by $5 \text{mm}$, which is motivated by the fact that this corresponds to half the area covered by a single valve and hence implies activation of the neighboring valve on both sides. With respect to enlargement in transport direction, we configure an individual parameter per product. This is motivated by the empirical observation that the deviations in velocity in transport direction $v_y$, i.e., down the chute, are noticeably larger for wooden plates than for lentils. For wooden plates, we extend the window time wise by $7.5 \text{ms}$ and for lentils by $2.2 \text{ms}$ before the start and after the end of the object as described by the estimated bounding box. As has been mentioned in Sec. I-B, enlarging the deflection pattern can be used to achieve more reliable deflections. However, it comes at the cost of increasing the risk of falsely co-deflecting objects located nearby and increases the amount of compressed air required.

C. Mechanical Parameters

The distance between the observation line of the line-scan camera and the separation is approximately $34 \text{mm}$. When using the area-scan camera, the pixel row located closest to the separation lies approximately $18 \text{mm}$ in front of it. As mentioned in Sec. II-A, the predicted deflection pattern of an object to be rejected is transmitted to the separation device whenever the estimated time remaining until reaching the separation stage falls below a certain threshold. In our system, this time threshold is formulated as a multiple $k$ of the duration of a single frame $t_{\text{frame}}$. The time threshold is then given by

$$\theta := kt_{\text{frame}}.$$  \hspace{1cm} (2)
Obviously, it is desirable to set the time threshold as small as possible in order to use the most recent information of an object for the calculation of the pattern. However, an existing delay in transmitting the information and physically activating a valve needs to be considered. The average distance \( \bar{d} \) of the last observation point to the separation is calculated by

\[
\bar{d} = \theta \bar{v_y},
\]

where \( \bar{v_y} \) denotes the average velocity in transport direction. In the following scenarios, \( \theta \) is set to 2.5, which approximately yields 26.9 ms for \( \theta \) and was determined empirically. Both for wooden plates and lentils, this yields \( \bar{d} \approx 47 \text{ mm} \) and hence a greater distance than the line-scan camera setup, which leads to a potential disadvantage. The distance between perception and separation together with the average velocity in transport direction can also be used to configure the delay for the line-scan camera system. For both products, dividing the distance by the mean velocity yields a delay of approximately 19 ms. However, an additional activation delay of the valves needs to be considered. Although vendors supply corresponding delay times, those are typically determined under very stable and ideal conditions, for instance regarding temperature, pressure, and power supply [50]. Therefore, the trigger delay was determined empirically for the system and was found to be around 3 ms. Hence, the delay configured is 16 ms.

Besides these separation related parameters, the angle of the chute has a large impact on transportation characteristics. For the experiments presented in this paper, the chute was mounted with an angle of 54°. This angle was found empirically to yield a good transportation of the products.

**D. Definition of Sorting Efficiency**

We adapt the definition of sorting efficiency from [41], [42] which is formulated as

\[
\text{Separation efficiency (SE) \%} := \frac{R_d - R_c}{R_d} \cdot 100,
\]

where \( R_d \) is the ratio of objects to be rejected and hence to be deflected that are located in the reject bin (true positive) in percent and \( R_c \) is the ratio of objects to be accepted that are also located in the reject bin (false positive) after the sorting process and hence were co-deflected in percent. In our definition, positive describes the test result for residues. The development of the key figure SE has recently been discussed in [51]. Obviously, in order to determine \( R_d \) and \( R_c \), the fraction of objects belonging to the accept and reject class needs to be determined per bin. In the course of this study, we re-apply the two separate bins after the sorting process on the sorting system and use the image processing algorithms to count the number of objects per class in the stream. The material is not separated again.

The outcome of the sorting process is not deterministic and is exposed to stochastic fluctuations. Various factors can impact the sorting efficiency even when keeping the parameters static. For instance, the material mixing is not identical when performing several runs, the mass flow can slightly vary, and so on. Such differences can also influence the proximity between objects, which is known to have an impact on the sorting efficiency [41]. Therefore, every experiment was repeated 20 times and statistics were calculated.

IV. EXPERIMENTAL RESULTS

Sorting results for wooden plates and lentils are illustrated in Fig. 10 and Fig. 11, respectively, and provided quantitatively in Table I. Regarding the discussion of results, it is emphasized that we are less interested in the absolute sorting efficiency but rather in a relative view, comparing the two system types.

Results for wooden plates using the small deflection pattern clearly reveal the disadvantage of using a static assumption regarding the separation delay when dealing with scenarios with high deviations in velocity. This disadvantage is clearly reflected in the performance of the line-scan camera system, see Fig. 10(a). The tracking system achieves considerably higher sorting performance in this case, quantitively by over 11 percentage points in average. This is due to a better outcome in \( R_d \). Results with respect to \( R_c \) are almost equal, see Table I. Enlarging the deflection pattern increases \( R_d \) for both system types, whereas the improvement is greater for the line-scan camera system, see Fig. 10(b). In average, \( R_d \) is increased by almost 12 percentage points for the line-scan camera based system and almost 3 percentage points for the tracking approach. The tracking system still achieves a higher sorting efficiency, however, the difference drops to just over 2 percentage points in average. Hence, the performances of the systems are getting closer to one another. However, this comes at the cost of higher energy consumption due to the increased usage of compressed air. For both system types, there exist experiments for which \( R_d > 90\% \) can be reported. Yet it also holds true that \( R_c \) is increased in this case.

Experiments carried out with lentils yield similar results. Yet, the difference in sorting efficiency is even bigger when using small deflection patterns, see Fig. 11(a), namely approximately 20 percentage points in average. The difference is again mainly due to superior results of the tracking system in \( R_d \). Employing large deflection patterns leads to convergence of the system’s performances as has been the case with wooden plates, see Fig. 11(b). Yet, the difference in mean sorting efficiency still lies around 7 percentage points in this case. In general, it appears that lentils are a harder sorting task than wooden plates. We do not elaborate further on this assumption but refer to the work presented in [49], which suggests that the mere smaller size of the objects may increase difficulty, as well as to the higher diversity in shape.

### Table I

<table>
<thead>
<tr>
<th>Product</th>
<th>Deflection pattern</th>
<th>System</th>
<th>( R_d )</th>
<th>( R_c )</th>
<th>SE</th>
<th>( \Delta \text{SE} )</th>
</tr>
</thead>
<tbody>
<tr>
<td>Plates</td>
<td>small</td>
<td>Line-scan</td>
<td>73.38</td>
<td>0.23</td>
<td>73.15</td>
<td>11.02</td>
</tr>
<tr>
<td></td>
<td>Tracking</td>
<td>Line-scan</td>
<td>84.53</td>
<td>0.36</td>
<td>84.17</td>
<td></td>
</tr>
<tr>
<td></td>
<td>Tracking</td>
<td>Tracking</td>
<td>86.00</td>
<td>1.20</td>
<td>84.80</td>
<td></td>
</tr>
<tr>
<td></td>
<td>Tracking</td>
<td>Tracking</td>
<td>88.29</td>
<td>1.51</td>
<td>86.78</td>
<td></td>
</tr>
<tr>
<td>Lentils</td>
<td>small</td>
<td>Line-scan</td>
<td>54.74</td>
<td>0.76</td>
<td>53.98</td>
<td>20.19</td>
</tr>
<tr>
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<td>Tracking</td>
<td>Line-scan</td>
<td>74.40</td>
<td>0.23</td>
<td>74.17</td>
<td></td>
</tr>
<tr>
<td></td>
<td>Tracking</td>
<td>Tracking</td>
<td>72.01</td>
<td>1.19</td>
<td>70.82</td>
<td></td>
</tr>
<tr>
<td></td>
<td>Tracking</td>
<td>Tracking</td>
<td>78.87</td>
<td>0.94</td>
<td>77.93</td>
<td>7.11</td>
</tr>
</tbody>
</table>
The distributions of the markers in Fig. 10 and Fig. 11 underline the previous statement that sorting results may vary from batch to batch. However, by repeating each experiment 20 times and taking the average, our results are stable enough to conclude that the sorting approach including an area-scan camera and tracking outperforms the conventional setup including a line-scan camera in each scenario. The increase in sorting efficiency is particularly high when working with small deflection patterns. This is of no surprise since large deflection patterns are a well-established measure taken to compensate imperfect flow control. In addition to the increased use of compressed air, it can also be observed from the results that enlarging the deflection pattern has a negative impact on $R_c$ as has been claimed before.

V. CONCLUSION

In this paper, we proposed an advanced image processing approach for decreasing the error in physical separation in sensor-based sorting. Our method enables reliable deflection of objects even at non-uniform velocities of individual objects. For this purpose, we proposed equipping a sorting system with an area-scan sensor and a predictive real-time multiobject tracking system. Based on experimentation with two different sorting tasks, we have shown that the proposed system outperforms a state-of-the-art reference system in every configuration under consideration. Sorting efficiency was increased by at least 2 percentage points and at most 20 percentage points. The increased efficiency is a result of the higher deflection accuracy. It was further shown that the proposed approach allows for employing small deflection patterns while retaining the sorting efficiency, which in turn lowers the required amount of compressed air and hence improves profitability and environmental friendliness.

The presented study revealed the necessity for accelerating computations of our advanced image processing system in order to achieve higher throughput for practical applications. Especially in case of the desired transfer from our experimental sorting system to an industrial sized system, real-time related issues might become more challenging since more objects need to be tracked, classified and separated simultaneously. Furthermore, our system not only provides information regarding where an object is moving but also how it is moving. We consider utilizing motion information for the identification of the materials in real sorting scenarios as proposed in [39], [40] to be a promising research direction.


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